

XALQARO NORDIK UNIVERSITETI

Iqtisodiyot va pedagogika fakulteti,
Iqtisodiyot va biznesni boshqarish kafedrası

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Mavzu: O'zgaruvchilar indikatoridan foydalanish

Reja:

1. O'zgaruvchilar indikatori
2. O'zgaruvchilar indikatorini qo'llash
3. Chiziqli ehtimollik model

7.1. O'zgaruvchilar indikatori

Indikator, yoki dummy model, o'zgaruvchilar ikkillik sanoq sistemasi 0/1 o'zgaruvchilari bo'lib, a ning mavjud yoki yoqligini harakterlaydi. Ushbu bo'limda biz ko'chmas mulk misolida o'zgaruvchi indikatorilaridan foydalanishni o'rganamiz. Yangi log faylini oching va *utown.dta* data faylini oching.

log using chap07_utown, replace text

use utown, clear

describe

summarize

Ma'lumotlarni va birinchi oltita kuzatuvni umumlashtiring.

list in 1/6

list in 501/506

“&” – bu mantiqiy amal bo’lib, ikki shart kiritilganda ularning har ikkisi shartga muvofiqligi yoki aksinchaligi ifodalash uchun ishlatiladi. Ya’ni kiritilgan ikki shart $PRICE > 215$ va $PRICE < 275$ lar har ikkisi ham to’g’ri bo’lsa, $MIDPRICE$ o’zgaruvchisining qiymati 1 ga teng bo’ladi. Quyida keltirilgan bir necha kuzatuvlarning natijalarini ko’rishingiz mumkin.

list sqft price large midprice in 1/5

. list sqft price large midprice in 1/5

	sqft	price	large	midprice
1.	23.46	205.452	0	0
2.	20.03	185.328	0	0
3.	27.77	248.422	1	1
4.	20.17	154.69	0	0
5.	26.45	221.801	1	1

7.1.2. O’zgaruvchilar indikatorining regressiyasini baholash

Aslida o’zgaruvchili indikatorli modellarni aniqlash (baholash) boshqa reggresiyalardan farq qilmaydi. Quyidagi modelni ko’rib chiqamiz:

$$PRICE = \beta_1 - \delta_1 UTOWN + \delta_2 SQFT + \gamma(SQFT * UTOWN) + \beta_3 AGE + \delta_2 POOL + \delta_3 FPLACE + e$$

Faktor o’zgaruvchisi yozuvidan foydalanish model

reg price i.utown sqft i.utown#c.sqft age i.pool i.fplace

Regressiya buyrug’i ya’ni *regress* qisqartirib *reg* shaklida qo’llaniladi. Bu Stata tez-tez ishlatiladigan buyruqlarni qisqartma shaklini qabul qilishiga yaqqol misol (masalan, *generate* buyrug’ini *gen* shaklda qo’llaniladi). Uzliksiz uchun omil o’zgaruvchisi *c*. faqatgina o’zgaruvchilarning o’zaro ta’sir etivchi holatlarda qo’llaniladi.

i.utown#c.sqft kiritmasi **UTOWN** va **SQFT** orasidagi o’zaro tasirni ifodalaydi. Biz Stata **A,B** va **A#B** larni qabul qilishi uchun “**A##B**” dan foydalanishimizning o’zi kifoya.

reg price i.utown##c.sqft age i.pool i.fplace

Hosil bo’ladigan natijada o’zgaruvchi indikatorini **UTOWN** *1.utown* kabi va o’zaro ta’sir koeffisienti iborasi **SQFT *UTOWN** *utown#c.sqft*. kabi nomoyon bo’ladi.

. reg price i.utown##c.sqft age i.pool i.fplace

Source	SS	df	MS			
Model	1548261.71	6	258043.619	Number of obs =	1000	
Residual	230184.426	993	231.807076	F(6, 993) =	1113.18	
Total	1778446.14	999	1780.22637	Prob > F =	0.0000	
				R-squared =	0.8706	
				Adj R-squared =	0.8698	
				Root MSE =	15.225	

	price	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
1.utown		27.45295	8.422582	3.26	0.001	10.92485 43.98106
sqft		7.612177	.2451765	31.05	0.000	7.131053 8.0933
utown#c.sqft						
1		1.299405	.3320478	3.91	0.000	.6478091 1.951001
age		-.1900864	.0512046	-3.71	0.000	-.2905681 -.0896048
1.pool		4.377163	1.196692	3.66	0.000	2.028828 6.725498
1.fplace		1.649176	.9719568	1.70	0.090	-.2581495 3.556501
_cons		24.49998	6.191721	3.96	0.000	12.34962 36.65035

7.1.3. O'zgaruvchilar indikatorining ahamiyatlilik testi

O'zgaruvchili indikator koeffisienti haqidagi gipotezalarini tekshirish boshqa koeffisientlar haqidagi gipotezalarni tekshirishdan farq qilmaydi. Unversitet shaxarchasining joylashuvining ahamiyatlilik testini o'tkazish uchun biz boshqa nolli bo'lmagan gipotezalarga qarshi $H_0: \delta_1 = 0, \gamma = 0$ nolli gipotezasini qo'yamiz.

Bu gipotezani F-testiga tekshirish uchun post-estimation buyrig'i yordamida amalga oshiriladi. Stata menyusining yuqorisidagi *Statistics>Postestimation >Tests>Test linear hypotheses* ketma-ketlikni amalga oshiring yoki regressiyadan so'ng test dialog oynasini ochish uchun *db test* ni kiriting. Stata buyrug'i esa quydagicha:

```
test 1.utown = 0 1.untown#c.sqft
```

Natija:

```
. test 1.utown 1.utown#c.sqft

( 1) 1.utown = 0
( 2) 1.utown#c.sqft = 0

F( 2, 993) = 1954.83
Prob > F = 0.0000
```

Sinov natijasi asosida, p-qiymati 0.0000 bilan, ahamiyatlilik darajasi $\alpha=0.05$ yoki hatto $\alpha=0.001$ bo'lmagan sababli biz nolli gipotezamizni inkor etamiz.

7.1.4. Qo'shimcha hisob-kitoblar

Uylarning unversitet oldida joylashuvining funksiyasining reggressiyasi quyidagicha hisoblanadi:

$$\widehat{PRICE} = (24.5+27.453) + (7.6122+1.2994)SQFT - .1901AGE + 4.3772POOL + 1.6492FPLACE = 51.953+89116SQFT - .1901AGE + 4.3772POOL + 1.6492FPLACE$$

Universitet yaqinida joylashgan uylar regressiya og'ishi va kesishishini aniqlash uchun *lincom* buyrug'idan foydalanamiz.

```
lincom _cons +1 .utown
```

```
lincom c.sqft + 1 .utown#c.sqft
```

natijalar nafaqat ehtimollikni ko'rsatadi balki ularning 95% ehtimollik orlig'ida ekanini ham ko'rsatadi.

```
. lincom _cons + 1.utown
```

```
( 1) 1.utown + _cons = 0
```

price	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
(1)	51.95294	5.767235	9.01	0.000	40.63557	63.2703

```
. lincom c.sqft + 1.utown#c.sqft
```

```
( 1) sqft + 1.utown#c.sqft = 0
```

price	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
(1)	8.911581	.2247944	39.64	0.000	8.470455	9.352708

7.1.5. O'rtacha marjinal ta'sirni hisoblash

Faktorli o'zgaruvchilarni yozma ko'rinishda foydalanishning yana bir qulaylik tomoni shundaki, marjinal effektlarni hisoblayotganda *margins* buyrug'idan to'g'ridan to'g'ri foydalaniladi:

margins, dydx()*

Natijada:

```
. margins, dydx(*)
```

```
Average marginal effects          Number of obs   =       1000
Model VCE      : OLS
```

```
Expression      : Linear prediction, predict()
dy/dx w.r.t.    : 1.utown sqft age 1.pool 1.fplace
```

	Delta-method			P> z	[95% Conf. Interval]	
	dy/dx	Std. Err.	z			
1.utown	60.21049	.9646176	62.42	0.000	58.31988	62.10111
sqft	8.286568	.1661803	49.86	0.000	7.96086	8.612275
age	-.1900864	.0512046	-3.71	0.000	-.2904456	-.0897272
1.pool	4.377163	1.196692	3.66	0.000	2.031691	6.722636
1.fplace	1.649176	.9719568	1.70	0.090	-.2558247	3.554176

Note: dy/dx for factor levels is the discrete change from the base level.

Yuqoridagi natija bu faqat Stata tomonidan chiqarilayotgan o'rtacha marjinal effektlarning qiymatidir. AGE, POOL va FPLACE uchun buni hisoblash mushkil emas. AGE uchun bu AGE ning PRICE ga marjinal ta'siridir, taxminiy koeffisientidir. POOL va FPLACE indikatorli o'zgaruvchilar bo'lganligi uchun ularning marjinal effekti hosil bo'lmaydi, balki birinchi navbatda hovuzga ega bo'lish yoki yo'qligi va ikkinchidan kaminga ega bo'lish yoki yo'qligi o'rtasidagi PRICening diskret o'zgarishidir. Shunday bo'lishiga qaramasdan *1.utown* va *sqft* uchun unchalik oddiy emas.

Ikki qo'shnilar o'rtasidagi kutilayotgan taklif etilayotgan PRICE farqlari quyidagicha:

$$(E(PRICE)|UTOWN=1) - (E(PRICE)|UTOWN=0) = \delta_1 + \gamma SQFT$$

Stata da quyidagicha hisoblaydi:

$$AME(UTOWN) = \frac{1}{N} \sum_{i=1}^N (\delta_1 + \gamma SQFT_1) = \delta_1 + \overline{\gamma SQFT}$$

Hisoblangan marjinal effektning dispersiyasi quyidagicha:

$$\text{var}(\widehat{AME}(UTOWN)) = \text{var}(\hat{\delta}_1 + \hat{\gamma} \overline{SQFT}) = \text{var}(\hat{\delta}_1) + \overline{SQFT}^2 \text{var}(\hat{\gamma}) + 2\overline{SQFT} \text{cov}(\hat{\delta}_1, \hat{\gamma})$$

Bu tog'riligini ko'rish uchun quyidagicha ishlarni amlaga oshiramiz:

quietly summarize sqft

scalar asqft = r(mean)

*lincom 1.utown+c.sqft#1.utown*asqft*

Natija esa:

```
. quietly summarize sqft
. scalar asqft = r(mean)
. lincom 1.utown+c.sqft#1.utown*asqft
( 1) 1.utown + 25.20965*1.utown#c.sqft = 0
```

price	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
(1)	60.21049	.9646176	62.42	0.000	58.31757	62.10342

Huddi shunday SQFT ning marjinal effektning ta'siri:

$$\frac{\partial E(PRICE)}{\partial SQFT} = \beta_2 + \gamma UTOWN$$

Stata quyidagicha hisoblaydi:

$$AME(SQFT) = \frac{1}{N} \sum_{i=1}^N \beta_2 + \gamma UTOWN_i = \beta_2 + \overline{\gamma UTOWN}$$

Hisoblash uchun quyidagicha amallarni bajaring:

quietly summarize utown

scalar autown = r(mean)

*lincom c.sqft+c.sqft#1.utown*autown*

```
. quietly summarize utown
. scalar autown = r(mean)
. lincom c.sqft+c.sqft#1.utown*autown
( 1) sqft + .519*1.utown#c.sqft = 0
```

price	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
(1)	8.286568	.1661803	49.86	0.000	7.960463	8.612673

log close

7.2. O'zgaruvchilar indikatorini qo'llash

Ushbu bo'limda biz indikator o'zgaruvchilarning turli xil ilovalarini ko'rib chiqamiz. *cps4_small.dta* data faylini oching. Yangi jurnalni ishga tushiring va ma'lumotlarni tekshiring.

log using chap07_cps4, replace text

use cps4_small, clear

describe

```
Contains data from cps4_small.dta
  obs:      1,000
  vars:      12
  size:     23,000 (99.9% of memory free)
```

variable name	storage type	display format	value label	variable label
wage	double	%10.0g		earnings per hour
educ	byte	%8.0g		years of education
exper	byte	%8.0g		post education years experience
hrswk	byte	%8.0g		usual hours worked per week
married	byte	%8.0g		= 1 if married
female	byte	%8.0g		= 1 if female
metro	byte	%8.0g		= 1 if lives in metropolitan area
midwest	byte	%8.0g		= 1 if lives in midwest
south	byte	%8.0g		= 1 if lives in south
west	byte	%8.0g		= 1 if lives in west
black	byte	%8.0g		= 1 if black
asian	byte	%8.0g		= 1 if asian

summarize

Natijada:

```
. summarize
```

Variable	Obs	Mean	Std. Dev.	Min	Max
wage	1000	20.61566	12.83472	1.97	76.39
educ	1000	13.799	2.711079	0	21
exper	1000	26.508	12.85446	2	65
hrswk	1000	39.952	10.3353	0	90
married	1000	.581	.4936423	0	1
female	1000	.514	.5000541	0	1
metro	1000	.78	.4144536	0	1
midwest	1000	.24	.4272968	0	1
south	1000	.296	.4567194	0	1
west	1000	.24	.4272968	0	1
black	1000	.112	.3155243	0	1
asian	1000	.043	.2029586	0	1

7.2.1. Sifat omillarining o'zaro ta'siri

Birinchi dan, biz modeldagi ikkita ko'rsatkich o'zgaruvchisi, qora va ayol o'rtasidagi o'zaro ta'sirni ko'rib chiqamiz.

$$WAGE = \beta_1 + \beta_2 EDUC + \delta_1 EDUC + \delta_2 BLACK + \delta_3 FEMALE + \gamma (BLACK \times FEMALE) + e$$

Faktorli o'zgaruvchilar operatoriga "###" yordamida regressiya hisoblanadi.

reg wage educ i.black##i.female

Eslatib o'tamiz, model quyidagicha:

$$WAGE = \beta_1 + \beta_2 EDUC + \beta_1 BLACK + \beta_1 FEMALE + \gamma (BLACK \times FEMALE) + e$$

Ya'ni

$$E(WAGE|FEMALE=1) = \beta_1 + \beta_2 EDUC + \beta_1 BLACK + \beta_2 + \gamma BLACK = (\beta_1 + \beta_2) + \beta_2 EDUC + (\beta_1 + \gamma) BLACK$$

va $E(WAGE|FEMALE=1) = \beta_1 + \beta_2 EDUC + \beta_1 BLACK$. Farqi esa quyidagicha:

$$E(WAGE|FEMALE=1) - E(WAGE|FEMALE=0) = \beta_2 + \gamma BLACK$$

Stata da quyidagicha natijaga topiladi:

$$AME(FEMALE) = \frac{1}{N} \sum_{i=1}^N (\hat{\delta}_2 + \hat{\gamma} BLACK_i) = \hat{\delta}_2 + \widehat{\gamma} \overline{BLACK}$$

Ayolning o'rtacha marjinal ta'sirini hisoblash quyidagi yordamida tekshiriladi.

quietly summarize black

scalar ablack = r(mean)

*lincom 1.female + 1.black#1.female*ablack*

. lincom 1.female + 1.black#1.female*ablack

(1) 1.female + .112*1.black#1.female = 0

wage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
(1)	-4.354046	.7313539	-5.95	0.000	-5.789219 -2.918873

7.2.2. Mintaqaviy o'zgaruvchilarni qo'shish

Keyin bir nechta toifali ko'rsatkich o'zgaruvchilari, mintaqaviy o'zgaruvchilar qo'shing. Modeli quyidagicha:

$$WAGE = \beta_1 + \beta_2 EDUC + \beta_3 BLACK + \beta_4 FEMALE + \beta_5 (BLACK \times FEMALE) + \delta_1 SOUTH + \delta_2 MIDWEST + \delta_3 WEST + e$$

Mintaqaviy indikator o'zgaruvchilari ma'lumotlar faylida allaqachon aniqlanganligi sababli, biz ularni regressiya modeliga shunchaki qo'shamiz.

reg wage educ i.black##i.female i.south i.midwest i.west

Natijaning bir qismi:

wage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
educ	2.071231	.1344687	15.40	0.000	1.807355 2.335106
1.black	-3.905465	1.786258	-2.19	0.029	-7.410743 -.4001873
1.female	-4.744129	.7698381	-6.16	0.000	-6.254827 -3.233431
black#female					
1 1	3.625021	2.318375	1.56	0.118	-.9244618 8.174504
1.south	-.4499056	1.025024	-0.44	0.661	-2.46137 1.561558
1.midwest	-2.608406	1.059644	-2.46	0.014	-4.687807 -.5290049
1.west	.9866332	1.059815	0.93	0.352	-1.093104 3.06637
_cons	-4.80621	2.028691	-2.37	0.018	-8.787229 -.8251912

Ushbu mintaqaviy o'zgaruvchining umumiy ahamiyatini tekshirish uchun *test* buyrug'idan foydalanimiz:

test 1.south 1.midwest 1.west

```
. test 1.south 1.midwest 1.west
```

```
( 1) 1.south = 0  
( 2) 1.midwest = 0  
( 3) 1.west = 0
```

```
F( 3, 992) = 4.25  
Prob > F = 0.0054
```

3 ta numerator va 992 bilan F-statistikadan kritik qiymatlarni hisoblang va maxraj erkinlik darajalari ko'rsating.

di "F(3,992,.95) = " invFtail(3,992,.05)

di "F(3,992,.90) = " invFtail(3,992,.10)

Natija:

```
. di "F(3,992,.95) = " invFtail(3,992,.05)  
F(3,992,.95) = 2.6138755  
. di "F(3,992,.90) = " invFtail(3,992,.10)  
F(3,992,.90) = 2.0893205
```

7.2.3. Ikki regressiya uchun tenglik testini o'tkazish

Janubiy mintaqa uchun ish haqi tenglamalarining qolgan qismiga nisbatan ekvivalentligini tekshirish mamlakat (ya'ni janubiy emas) biz regressiya modelidagi har bir o'zgaruvchi uchun janubiy ko'rsatkich o'zgaruvchisi bilan o'zaro ta'sir o'zgaruvchisini yaratamiz. Biz sinab ko'rmoqchi bo'lgan tenglama quyidagicha:

$$WAGE = \beta_1 + \beta_2 EDUC + \beta_3 BLACK + \beta_4 FEMALE + \gamma (BLACK \times FEMALE) + e$$

Indikator o'zgaruvchan o'zaro ta'sirga ega model quyidagicha ko'rinishda

$$WAGE = \beta_1 + \beta_2 EDUC + \beta_3 BLACK + \beta_4 FEMALE + \gamma (BLACK \times FEMALE) + \theta_1 SOUTH + \theta_2 (EDUC \times SOUTH) + \theta_3 (BLACK \times SOUTH) + \theta_4 (FEMALE \times SOUTH) + \theta_5 (BLACK \times FEMALE \times SOUTH) + e$$

Biz SOUTH bilan regressiya modelidagi har bir o'zgaruvchi bilan, kesishuvchi o'zaro ta'sir bo'yicha ish olib bordik. ## Stata operatoridan foydalanib barcha o'zaro tasir etuvchilarni yarating. Avvalo, BLACK, FEMALE va ularning o'zaro ta'sir etuvchilarini yaratishda biz *i.black##i.female*. dan foydalanamiz. So'ng to'liq o'zaro ta'sir modelini yaratamiz

reg wage i.south##(c.educ i.black##i.female)

Natija esa:

```
. reg wage i.south##(c.educ i.black##i.female)
```

Source	SS	df	MS			
Model	34581.0189	9	3842.33543	Number of obs =	1000	
Residual	129984.409	990	131.297383	F(9, 990) =	29.26	
Total	164565.428	999	164.730158	Prob > F =	0.0000	
				R-squared =	0.2101	
				Adj R-squared =	0.2030	
				Root MSE =	11.459	

wage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
1.south	3.94391	4.048453	0.97	0.330	-4.000625	11.88845
educ	2.172554	.1664639	13.05	0.000	1.845891	2.499216
1.black	-5.08936	2.64306	-1.93	0.054	-10.276	.0972837
1.female	-5.005078	.8990074	-5.57	0.000	-6.769257	-3.240899
black#female						
1 1	5.305574	3.497267	1.52	0.130	-1.557333	12.16848
south#c.educ						
1	-.308541	.2857343	-1.08	0.280	-.8692554	.2521734
south#black						
1 1	1.704396	3.633327	0.47	0.639	-5.42551	8.834302
south#female						
1 1	.9011198	1.772665	0.51	0.611	-2.577492	4.379732
south#black#						
female						
1 1 1	-2.935834	4.787647	-0.61	0.540	-12.33094	6.459268
_cons	-6.605572	2.336628	-2.83	0.005	-11.19088	-2.02026

Janubiy va qolgan qismi uchun model o'rtasida "hech qanday farq" yo'qligi haqidagi gipotezani sinab ko'rish uchun mamlakat $H_0 : \theta_1 = \theta_2 = \theta_3 = \theta_4 = \theta_5 = 0$ qo'shma gipotezasini *test* bayonoti yordamida tekshiramiz.

```
test 1.south 1.south#c.educ 1.south#1.black 1.south#1.female ///  
1.south#1.black#1.female
```

Natija:

```
. test 1.south 1.south#c.educ 1.south#1.black 1.south#1.female ///
```

- ```
> 1.south#1.black#1.female
```
- ( 1) 1.south = 0
  - ( 2) 1.south#c.educ = 0
  - ( 3) 1.south#1.black = 0
  - ( 4) 1.south#1.female = 0
  - ( 5) 1.south#1.black#1.female = 0

```
F(5, 990) = 0.32
Prob > F = 0.9009
```

To'liq o'zaro ta'sirlar modelidan biz QORA va JANUBIY o'zgaruvchilar yordamida birgalikdagi effektini olishimiz mumkin.

*lincom 1.black + 1.black#1.south*

Natija quyidagicha:

```
. lincom 1.black + 1.black#1.south
(1) 1.black + 1.south#1.black = 0
```

| wage | Coef.     | Std. Err. | t     | P> t  | [95% Conf. Interval] |          |
|------|-----------|-----------|-------|-------|----------------------|----------|
| (1)  | -3.384964 | 2.49305   | -1.36 | 0.175 | -8.277233            | 1.507305 |

Xuddi shunday, AYOL va SOUTHning birgalikdagi ta'siri yordamida:  
***lincom 1.female + 1.female#1.south***

Natija:

```
. lincom 1.female + 1.female#1.south
(1) 1.female + 1.south#1.female = 0
```

| wage | Coef.     | Std. Err. | t     | P> t  | [95% Conf. Interval] |           |
|------|-----------|-----------|-------|-------|----------------------|-----------|
| (1)  | -4.103958 | 1.527785  | -2.69 | 0.007 | -7.102027            | -1.105889 |

#### 7.2.4. Alohida regressiyalarni baholash

Oldingi bo'limda to'liq o'zaro ta'sirlangan model yondashuvidan foydalanish o'rniga, F-statistik bo'lishi mumkin kvadrat qoldiqlarning cheklangan va cheklanmagan yig'indisi yordamida hisoblangan. Kvadrat yig'indisi to'liq model uchun qoldiqlar ikkita alohida regressiyadan olingan SSE yig'indisidir.

$$SSE_{full} = SSE_{non-south} + SSE_{south} = 89088.5 + 40895.9 = 129984.4$$

Ikki mintaqa bo'yicha hisob-kitoblar standart regress yordamida *bysort* buyrug'i bilan samarali amalga oshirilishi mumkin, bu Stata buyruqlarini ma'lumotlarning kichik to'plamlarida takrorlash imkonini beradi. *help bysort* ni kiriting. By prefiksdan foydalanish uchun ma'lumotlarni guruhlash o'zgaruvchisi yoki o'zgaruvchilari bo'yicha tartiblash kerak. Agar bu hali bajirmagan bo'lsa, *by* va *sort* buyriqlarini *bysort* shaklida kiriting. Sintaksis buyruqlari quyidagicha:

***by varlist: stata\_cmd***

***bysort varlist: stata\_cmd***

Ikki mintaqa uchun regressiyalarni amalga oshirish uchun bizda mavjud:

***bysort south: reg wage educ i.black##i.female***

Ya'ni, biz avval SOUTH qiymatlari bo'yicha tartiblaymiz va keyin har bir kuzatish guruhi uchun regressiyani amalga oshiramiz.

. bysort south: reg wage educ i.black##i.female

-> south = 0

| Source   | SS         | df  | MS         |                 |        |  |
|----------|------------|-----|------------|-----------------|--------|--|
| Model    | 25346.0083 | 4   | 6336.50209 | Number of obs = | 704    |  |
| Residual | 89088.4615 | 699 | 127.451304 | F( 4, 699) =    | 49.72  |  |
| Total    | 114434.47  | 703 | 162.780185 | Prob > F =      | 0.0000 |  |
|          |            |     |            | R-squared =     | 0.2215 |  |
|          |            |     |            | Adj R-squared = | 0.2170 |  |
|          |            |     |            | Root MSE =      | 11.289 |  |

  

| wage                | Coef.     | Std. Err. | t     | P> t  | [95% Conf. Interval] |           |
|---------------------|-----------|-----------|-------|-------|----------------------|-----------|
| educ                | 2.172554  | .1640077  | 13.25 | 0.000 | 1.850547             | 2.49456   |
| 1.black             | -5.08936  | 2.604061  | -1.95 | 0.051 | -10.20208            | .0233585  |
| 1.female            | -5.005078 | .8857423  | -5.65 | 0.000 | -6.744112            | -3.266044 |
| black#female<br>1 1 | 5.305574  | 3.445664  | 1.54  | 0.124 | -1.459516            | 12.07066  |
| _cons               | -6.605572 | 2.30215   | -2.87 | 0.004 | -11.12553            | -2.085615 |

-> south = 1

| Source   | SS         | df  | MS         |                 |        |  |
|----------|------------|-----|------------|-----------------|--------|--|
| Model    | 9234.26014 | 4   | 2308.56503 | Number of obs = | 296    |  |
| Residual | 40895.9474 | 291 | 140.535902 | F( 4, 291) =    | 16.43  |  |
| Total    | 50130.2075 | 295 | 169.932907 | Prob > F =      | 0.0000 |  |
|          |            |     |            | R-squared =     | 0.1842 |  |
|          |            |     |            | Adj R-squared = | 0.1730 |  |
|          |            |     |            | Root MSE =      | 11.855 |  |

  

| wage                | Coef.     | Std. Err. | t     | P> t  | [95% Conf. Interval] |          |
|---------------------|-----------|-----------|-------|-------|----------------------|----------|
| educ                | 1.864013  | .2402682  | 7.76  | 0.000 | 1.391129             | 2.336896 |
| 1.black             | -3.384964 | 2.579268  | -1.31 | 0.190 | -8.46135             | 1.691422 |
| 1.female            | -4.103958 | 1.580621  | -2.60 | 0.010 | -7.214857            | -.993059 |
| black#female<br>1 1 | 2.36974   | 3.382739  | 0.70  | 0.484 | -4.287995            | 9.027476 |
| _cons               | -2.661662 | 3.420413  | -0.78 | 0.437 | -9.393547            | 4.070223 |

Ikki SSE alohida regressiyalardan dispersiya jadvalining tahlilidan kelib chiqadi.

### 7.2.5. Log-chiziqli modellariga o'zgaruvchilar indikatorining qo'llanilishi

Log-chiziqli modeldagi indikator o'zgaruvchisining aniq ta'sirini hisoblash murakkab ko'rinadi, ammo Stataning *nlcom* buyrug'i buni ancha osonlashtiradi.

*ln(wage)* tuzing va quyidagi tenglamani hisoblang:

$$\ln(WAGE) = \beta_1 + \beta_2 EDUC + \delta FEMALE$$

*gen lwage = ln(wage)*

*reg lwage educ i.female*

Natija quyidagicha:

. reg lwage educ i.female

| Source   | SS         | df  | MS         |                 |        |  |
|----------|------------|-----|------------|-----------------|--------|--|
| Model    | 74.5420655 | 2   | 37.2710328 | Number of obs = | 1000   |  |
| Residual | 262.238666 | 997 | .263027749 | F( 2, 997) =    | 141.70 |  |
| Total    | 336.780731 | 999 | .337117849 | Prob > F =      | 0.0000 |  |
|          |            |     |            | R-squared =     | 0.2213 |  |
|          |            |     |            | Adj R-squared = | 0.2198 |  |
|          |            |     |            | Root MSE =      | .51286 |  |

  

| lwage    | Coef.    | Std. Err. | t     | P> t  | [95% Conf. Interval] |           |
|----------|----------|-----------|-------|-------|----------------------|-----------|
| educ     | .0962484 | .0060365  | 15.94 | 0.000 | .0844026             | .1080942  |
| 1.female | -.243214 | .0327275  | -7.43 | 0.000 | -.3074367            | -.1789913 |
| _cons    | 1.653868 | .0843786  | 19.60 | 0.000 | 1.488288             | 1.819448  |

Ko'rsatkichning aniq ta'siri va indikatorli o'zgaruvchisi:

$$100(e^{\delta} - 1)\%$$

Bu *nlcom*.dan foydalanishni talab qiluvchi parametrlarning chiziqli bo'lmagan funktsiyasi:

$$nlcom.100*(exp(_b[1.female]) - 1) \quad 100*(exp(_b[1.female]) - 1)$$

Buning natijasi:

```
. nlcom 100*(exp(_b[1.female]) - 1)
 _nl_1: 100*(exp(_b[1.female]) - 1)
```

| lwage | Coef.     | Std. Err. | t     | P> t  | [95% Conf. Interval] |          |
|-------|-----------|-----------|-------|-------|----------------------|----------|
| _nl_1 | -21.58963 | 2.566176  | -8.41 | 0.000 | -26.62535            | -16.5539 |

Ya'ni, qolgan hamma narsani o'zgarmagan holda, biz ayol ishchilar erkaklarnikiga qaraganda 21,6% kamroq maosh olishlarini taxmin qilamiz.

Xuddi shunday, biz boshqa chiziqli bo'lmagan marjinal effektlarni hisoblashimiz mumkin. Modelni ko'rib chiqamiz.

$$\ln(WAGE) = \beta_1 + \beta_2 EDUC + \beta_3 EXPER + \gamma(EDUC * EXPER)$$

Taxminiy marjinal ta'sir

$$100(\beta_3 + \gamma EDUC)\%$$

Ta'lim va tajribaning o'zaro ta'sirini yarating va uni regressiya modeliga qo'shing

$$reg lwage c.educ##c.exper$$

Baholash natijalari:

```
. reg lwage c.educ#c.exper
```

| Source   | SS         | df  | MS         |                 |        |  |
|----------|------------|-----|------------|-----------------|--------|--|
| Model    | 65.5449479 | 3   | 21.848316  | Number of obs = | 1000   |  |
| Residual | 271.235783 | 996 | .272325084 | F( 3, 996) =    | 80.23  |  |
| Total    | 336.780731 | 999 | .337117849 | Prob > F =      | 0.0000 |  |
|          |            |     |            | R-squared =     | 0.1946 |  |
|          |            |     |            | Adj R-squared = | 0.1922 |  |
|          |            |     |            | Root MSE =      | .52185 |  |

  

| lwage              | Coef.     | Std. Err. | t     | P> t  | [95% Conf. Interval] |          |
|--------------------|-----------|-----------|-------|-------|----------------------|----------|
| educ               | .0949385  | .0146246  | 6.49  | 0.000 | .06624               | .123637  |
| exper              | .0063295  | .0066985  | 0.94  | 0.345 | -.0068153            | .0194743 |
| c.educ#<br>c.exper | -.0000364 | .0004838  | -0.08 | 0.940 | -.0009858            | .0009129 |
| _cons              | 1.392318  | .2066447  | 6.74  | 0.000 | .986809              | 1.797827 |

Lincom yoki *nlcom*-dan foydalanish uchun *\_b [o'zgaruvchi]* ko'rinishidagi koeffitsient nomlari ba'zan faktor belgilaridan foydalanganda darhol aniqlanmaydi. Buni koeffitsientlar jadvalini emas, balki *coeflegend* afsonasini ko'rsatadigan variant koeflegendasi bilan *regress* buyrug'ini ko'rsatish orqali aniqlash mumkin.

### *reg, coeflegend*

```
. reg, coeflegend
```

| Source   | SS         | df  | MS         |                 |        |  |
|----------|------------|-----|------------|-----------------|--------|--|
| Model    | 65.5449479 | 3   | 21.848316  | Number of obs = | 1000   |  |
| Residual | 271.235783 | 996 | .272325084 | F( 3, 996) =    | 80.23  |  |
| Total    | 336.780731 | 999 | .337117849 | Prob > F =      | 0.0000 |  |
|          |            |     |            | R-squared =     | 0.1946 |  |
|          |            |     |            | Adj R-squared = | 0.1922 |  |
|          |            |     |            | Root MSE =      | .52185 |  |

  

| lwage              | Coef.     | Legend             |
|--------------------|-----------|--------------------|
| educ               | .0949385  | _b[educ]           |
| exper              | .0063295  | _b[exper]          |
| c.educ#<br>c.exper | -.0000364 | _b[c.educ#c.exper] |
| _cons              | 1.392318  | _b[_cons]          |

Taxminiy va aniq effektlar yordamida hisoblab chiqiladi

*lincom 100\*(exper+ c.educ#c.exper\*16)*

```
. lincom 100*(exper+ c.educ#c.exper*16)
```

( 1) 100\*exper + 1600\*c.educ#c.exper = 0

| lwage | Coef.   | Std. Err. | t    | P> t  | [95% Conf. Interval] |          |
|-------|---------|-----------|------|-------|----------------------|----------|
| (1)   | .574639 | .174402   | 3.29 | 0.001 | .2324014             | .9168765 |

*nlcom 100\*(exp( \_b[exper]+\_b[c.educ#c.exper]\*16) - 1)*

```
. nlcom 100*(exp(_b[exper]+_b[c.educ#c.exper]*16) - 1)
 _nl_1: 100*(exp(_b[exper]+_b[c.educ#c.exper]*16) - 1)
```

| lwage | Coef.    | Std. Err. | t    | P> t  | [95% Conf. Interval] |         |
|-------|----------|-----------|------|-------|----------------------|---------|
| _nl_1 | .5762932 | .1754071  | 3.29 | 0.001 | .2320833             | .920503 |

*log close*

### 7.3. Chiziqli empirik model

Ikki muqobil o'rtasida tanlovni modellashtirishda indikator o'zgaruvchisi bog'liq bo'ladi, regressiya modelida mustaqil o'zgaruvchi emas, balki erksiz o'zgaruvchi. Faraz qilaylik:

$$Y = \begin{cases} 1 & \text{birinchi muqobil tanlansa} \\ 0 & \text{agar ikkinchi variant tanlansa} \end{cases}$$

Agar p birinchi muqobil tanlanish ehtimoli bo'lsa, u holda  $P[y=1]=p$  bo'lsa, y ning kutilayotgan qiymati  $E(y) = p$ , dispersiyasi esa  $var(y)=p(p-1)$  bo'ladi.

Biz chiziqli regressiya funksiyasidan yoki shu nuqtai nazardan chiziqli ehtimollik modelidan foydalangan holda p ehtimolligiga ta'sir etuvchi omillarni aniqlashdan manfaatdormiz.

$$E(y) = p = \beta_1 + \beta_2 x_2 + \dots + \beta_K x_K$$

Chiziqli ehtimollik regressiya modeli:

$$y = \beta_1 + \beta_2 x_2 + \dots + \beta_K x_K + e$$

Xato atamasining dispersiyasi e ga teng.

$$var(e) = (\beta_1 + \beta_2 x_2 + \dots + \beta_K x_K)(1 - \beta_1 - \beta_2 x_2 - \dots - \beta_K x_K)$$

Bu xato homosedastik emas va buni 8-bobda to'liq ko'rib chiqamiz.

Misol sifatida Cola va Pepsi o'rtasidagi tanlovni ko'rib chiqing. *Coke.dta* ni oching va uning mazmunini tekshiring.

*log using chap07\_coke, replace text*

*use coke, clear*

*describe*

*summarize*

| variable name | storage type | display format | value label | variable label                                               |
|---------------|--------------|----------------|-------------|--------------------------------------------------------------|
| coke          | byte         | %8.0g          |             | =1 if coke chosen, =0 if pepsi chosen                        |
| pr_pepsi      | double       | %10.0g         |             | price of 2 liter bottle of pepsi                             |
| pr_coke       | double       | %10.0g         |             | price of 2 liter bottle of coke                              |
| disp_pepsi    | byte         | %8.0g          |             | = 1 if pepsi is displayed at time of purchase, otherwise = 0 |
| disp_coke     | byte         | %8.0g          |             | = 1 if coke is displayed at time of purchase, otherwise = 0  |
| pratio        | double       | %10.0g         |             | price of coke relative to price of pepsi                     |

Eng kichik kvadratlar regressiyasidan foydalanib, kola tanlash uchun chiziqli ehtimollik modelini taxmin qilamiz.



## *reg coke pratio disp\_coke disp\_pepsi*

```
. reg coke pratio disp_coke disp_pepsi
```

| Source   | SS         | df   | MS         |  |  |  |
|----------|------------|------|------------|--|--|--|
| Model    | 33.8378078 | 3    | 11.2792693 |  |  |  |
| Residual | 248.004297 | 1136 | .218313642 |  |  |  |
| Total    | 281.842105 | 1139 | .247446976 |  |  |  |

  

|            | Coef.     | Std. Err. | t     | P> t  | [95% Conf. Interval] |
|------------|-----------|-----------|-------|-------|----------------------|
| pratio     | -.4008614 | .0613494  | -6.53 | 0.000 | -.5212324 -.2804904  |
| disp_coke  | .0771745  | .0343919  | 2.24  | 0.025 | .0096956 .1446533    |
| disp_pepsi | -.1656637 | .0355997  | -4.65 | 0.000 | -.2355122 -.0958152  |
| _cons      | .8902151  | .0654849  | 13.59 | 0.000 | .7617301 1.0187      |

Number of obs = 1140  
F( 3, 1136) = 51.67  
Prob > F = 0.0000  
R-squared = 0.1201  
Adj R-squared = 0.1177  
Root MSE = .46724

Chiziqli regressiya yondashuvi bilan bog'liq tashvish shundaki, bashorat qilingan ehtimolliklar [0, 1] oraliqdan tashqarida bo'lishi mumkin. Bu holda ehtimollik bo'lgan bashorat qilingan qiymatlarni oling va umumlashtiring.

### *predict phat*

### *summarize phat*

```
. summarize phat
```

| Variable | Obs  | Mean     | Std. Dev. | Min       | Max      |
|----------|------|----------|-----------|-----------|----------|
| phat     | 1140 | .4473684 | .1723611  | -.2073211 | .7680784 |

Biz minimal qiymat noldan kichik ekanligini ko'ramiz, lekin bashorat qilingan ehtimollarning hech biri birdan katta emas. Qancha bashorat qilingan ehtimollar salbiy ekanligini ko'rish uchun ulardan foydalanib, ularni umumlashtiring

### *summarize phat if phat<=0*

```
. summarize phat if phat<=0
```

| Variable | Obs | Mean      | Std. Dev. | Min       | Max       |
|----------|-----|-----------|-----------|-----------|-----------|
| phat     | 16  | -.0183585 | .0523201  | -.2073211 | -.0002385 |

1140 ta kuzatuvdan 16 tasi salbiy bashorat qilingan ehtimollarga ega ekanligini ko'ramiz.

### *log close*

## **VII bob mavzularini mustahkamlash uchun savollar**

1. O'zgaruvchilar indikatori deganda nimani tushumasiz?
2. O'zgaruvchilarning qiymatlariga asoslangan holda yangi indikatorli o'zgaruvchilarni hosil qilish uchun qanday buyruqdan foydalaniladi?
3. Yakuniy satatistik xulosaning har bir detalalarini hisoblash uchun qaysi buyruqlardan foydalanish lozim?
4. O'zgaruvchili indikator koeffisienti gipotezalarini tekshirish uchun qanday buyruqlarni bajarish talab etiladi?
5. O'rtacha marjinal ta'sirni hisoblash buyrug'ini ifodalang.
6. indikator o'zgaruvchilarini ifodalashda qanday fayl orqali amalga oshiriladi?
7. Mintaqaviy indikator o'zgaruvchilari ma'lumotlarini regressiya modeliga kiritish uchun qanday amallar bajarilishi lozim?
8. Ikki mintaqa bo'yicha hisob-kitoblar qaysi buyruq yordamida amalga oshiriladi?
9. Chiziqli empirik model tuzish qanday amallarni bajarishni talab etadi?
10. Chiziqli ehtimollik regressiya modelini ifodalang.